

Depth-mapping of refractive index and sound velocity in transparent samples by time-domain Brillouin Scattering

Motonobu Tomoda^{1†}, Akihisa Kubota¹, Osamu Matsuda¹, Yoshihiro and Oliver B. Wright^{1,2} (¹Grad School Eng., Hokkaido Univ.; ²Grad School Eng., Osaka Univ.)

1. Introduction

Time-domain Brillouin scattering is an all-optical experimental technique that makes use of laser picosecond ultrasonics to investigate transparent materials.¹⁾ The time-resolved optical reflectance exhibits GHz oscillations resulting from the interference between probe light pulses reflected from the sample interfaces and those scattered from nano-acoustic pulses, as illustrated in **Fig. 1(a)**. These oscillations, known as Brillouin oscillations, occur at the frequency

$$f_B = 2v\sqrt{n^2 - \sin^2 \theta_0}/\lambda, \quad (1)$$

where v is the longitudinal sound velocity, n is the refractive index, θ_0 is the incident angle of the probe light in air, and λ is the probe-light wavelength in air. When the refractive index of the sample is spatially uniform and known, analysing the oscillations using Short-Time Fourier Transforms (STFT) enables the acquisition of depth profiles of v . However, when the refractive index varies with depth, multiple incidence angles of the probe beam are required, thereby complicating the measurement system.²⁾

In this study, we propose a straightforward method to obtain quantitative 3-dimensional (3D) images of v and n by varying the incident angle of the probe light.³⁾ By scanning the incidence position of a narrow probe beam on a high numerical aperture (NA) objective lens, Brillouin oscillations can be measured from different oblique incidence angles θ_0 .

2. Experiment and results

When the collimated narrow beam propagates parallel to the center axis of the microscope objective, but with an off-axis displacement x and y , the incident angle on the sample is

$$\theta_0 = \tan^{-1}(\sqrt{x^2 + y^2}/F), \quad (2)$$

where F is the focal length, as illustrated in **Fig. 1(b)**.

In order to validate the effectiveness of this technique, we select a water-immersion microscope objective (NA=1.0, $F=3.0$ mm, working distance 2

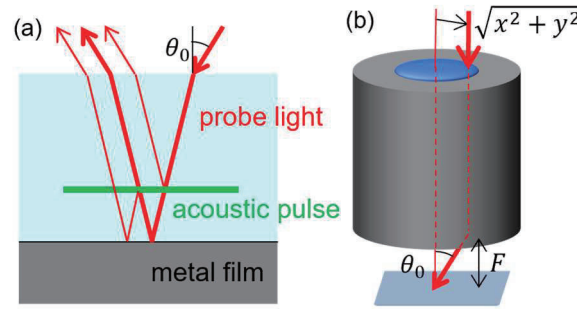


Fig. 1 (a) Schematic showing the interference of probe light components to produce Brillouin oscillations. (b) Schematic showing the relation between the incidence off-axis displacement x and y and the output angle θ_0 of a narrow beam entering a microscope objective with focal length F .

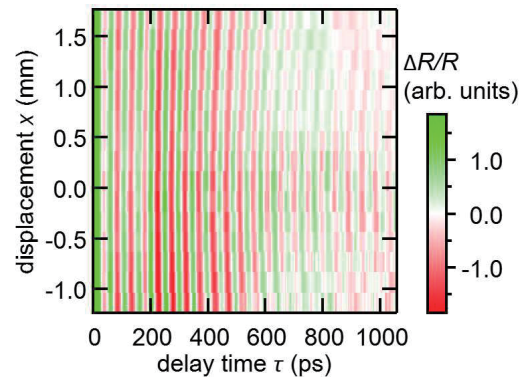


Fig. 2 Probe-beam relative reflectance change as a function of the delay time and the probe beam lateral off-axis displacement on the objective lens.

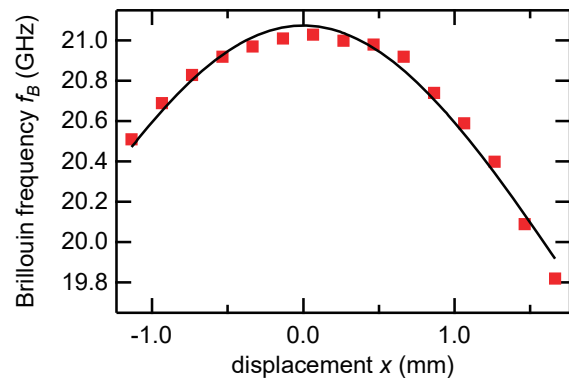


Fig. 3 Frequency of the Brillouin oscillations derived from temporal Fourier transforms of the experimental data (red points) and fitted curve (black solid line).

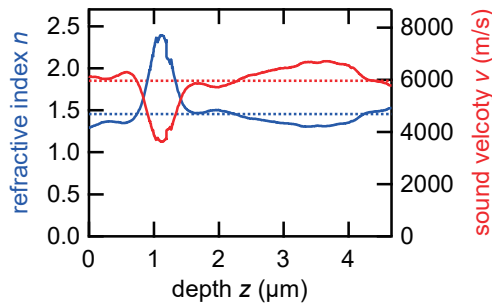


Fig. 4 Derived refractive index (blue solid line) and longitudinal sound velocity (red solid line) in silica sample as a function of depth. The dotted lines represent the expected values.

mm) for focusing and an isotropic fused silica cover glass coated on one side with a titanium film of thickness 640 nm for the sample.

Relative reflectance changes $\Delta R/R$ of the probe light are detected, the results being shown in **Fig. 2**, where Brillouin oscillations at approximately 20 GHz are clearly visible. **Figure 3** shows the frequency of these Brillouin oscillations (red squares) obtained by temporal Fourier transforms over 1000 ps as a function of x . The solid line is obtained by least-squares fitting to the experimental data with Eqs. (1) and (2) using the focal length F and displacement y as variable parameters, and under the assumption that n and v take their literature values $n=1.45$ and $v=5967$ m/s. The fitted average values of $F=3.05$ mm and $y=0.38$ mm are of the expected order of magnitude.

By performing STFT on the data for each off-axis displacement x , we obtain f_B for each delay time τ . Through least-squares fitting at each τ and using the fitted values $F=3.05$ mm and $y=0.38$ mm from the data of Fig. 3, we calculate the values of v and n . Then τ is converted into depth z by use of the derived value of v , which enables the acquisition of depth profiles as shown in **Fig. 4**. The variations in n and v extracted from our measurements exhibit agreement with the expected values (dotted lines), except for the artifact region around $z=1.2$ μm , which arises because of the bouncing of acoustic pulses to and fro inside the Ti film.

3. Conclusions

We present a technique in time-domain Brillouin scattering for the depth profiling of both sound velocity and refractive index in a transparent material based on automated optical probe-incidence scanning. This allows incident-angle resolved measurements in a compact system without the need for a cumbersome optical arrangement. This technique is validated with a well-characterized homogeneous glass sample, but it should be applicable to mapping sound velocities, dependent on stiffness, in 3D in a variety of inhomogeneous transparent samples.

A different method in time-domain Brillouin scattering for extracting sound velocity without a knowledge of the refractive index was recently proposed by us,⁴⁾ which makes use of probe light obliquely incident on a side face—as opposed to the usual top face—of the sample. In the presentation at the symposium, we introduce the comparison of these two methods.

Acknowledgment

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References

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